

Aileen Michaels

EN – SEMI – MODELS

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Let $\underline{A} = \langle A, -, \circ, \dots \rangle$ be an algebra similar to the language of the EN -logic. The unary operation $-$ and binary operation \circ correspond to the connective of truth-functional negation and identity connective, respectively. Compare this Bulletin.

If $D \subseteq A$ and for all $a, b \in A$:

- (1) $(-a) \in D$ iff $a \notin D$
- (2) $(a \circ b) \in D$ iff $a = b$

then the pair $\langle \underline{A}, D \rangle$ is called (normal) EN -model. Notice that the condition (1) implies maximality of D . In fact if both D_1 and D_2 satisfy (1) and $D_1 \subseteq D_2$ then $D_1 = D_2$. Algebra \underline{A} is said to be an EN -semi-model if there exists $D \subseteq A$ such that $\langle \underline{A}, D \rangle$ is an EN -model.

We will use the expression $-[k](a)$ to denote $\overbrace{- \dots -}^k a$ for each $a \in A$ and $k = 0, 1, 2, \dots$

THEOREM. *Algebra \underline{A} is an EN -semi-model if and only if for all $a, b, c \in A$ and $i, j = 0, 1, 2, \dots$:*

- (3) $-[2i + 1](a) \neq -[2j](a)$
- (4) *if $b \neq c$ then both $-[2i](a \circ a) \neq -[2j](b \circ c)$
and $-[2i + 1](a \circ a) \neq -[2j + 1](b \circ c)$*

COROLLARY. The class of all EN-semi-models is axiomatic with respect to the first order logic. On the other hand, the class of all EN-models is easily seen to be elementary with respect to that logic. For the notions involved see G. Grätzer, Universal Algebra, D. Van Nostrand 1968, chapter 42.

*Stevens Tnstitute of Technology
Hoboken, N.Y., USA*